

of model solids characterizing the elasticity of those materials. In transforming the elasticity of the Earth into solid-state parameters of composition, pressure, and temperature, the properties needed are the intrinsic elastic properties of earth materials (not the apparent properties as one measures on a porous sample).

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Notation

<i>Symbols</i>	<i>Units</i>	<i>Meaning</i>
V_p	km/sec	Velocity of compressional waves
V_p^0	km/sec	Velocity of compressional waves at zero-porosity
V_s	km/sec	Velocity of shear waves
V_s^0	km/sec	Velocity of shear waves at zero-porosity
V_j	km/sec	Velocity of j th mode
M_j	kb	Elastic modulus of j th mode
M_j^0	kb	Elastic modulus of j th mode at zero-porosity
L_s	kb	Longitudinal modulus given by $(\text{density} \times V_p^2)$
L_s^0	kb	Longitudinal modulus at zero-porosity
μ	kb	Shear modulus
μ^0	kb	Shear modulus at zero-porosity
K_s	kb	Adiabatic bulk modulus
K_s^0	kb	Adiabatic bulk modulus at zero-porosity
K_T	kb	Isothermal bulk modulus
K_T^0	kb	Isothermal bulk modulus at zero-porosity
Y	kb	Young's modulus
σ_s	None	Poisson's ratio
σ_s^0	None	Poisson's ratio at zero-porosity
f_j	Hz/sec	Pulse-repetition frequency (PRF) of j th mode

f_p	Hz/sec	PRF of compressional mode
f_s	Hz/sec	PRF of shear mode
P	None	Compressional mode
S	None	Shear mode
a	None	Aspect ratio
p	kb	Pressure
T	°K	Temperature
α	per °K	Coefficient of volume expansion
θ	None	Volume fraction of pores.

References

- [1] W.B. Crandall, D.H. Chung, and T.J. Gray, Mechanical properties of fine-grained hot-pressed alumina, Chapter 22, in: *Mechanical Properties of Engineering Ceramics*, eds. W. Kriegel and H. Palmour (Interscience, New York 1961), 349-379.
- [2] D.H. Chung, Elastic and anelastic properties of fine-grained polycrystalline alumina, *Bull. Ceram. Res.* 26 (1961) 1-87.
- [3] O.L. Anderson, A simplified method for calculating the Debye temperature from elastic constants, *J. Phys. Chem. Solids* 24 (1963) 909-917.
- [4] O.L. Anderson, Determination and some uses of isotropic elastic constants of polycrystalline aggregates, using single-crystal data, Chapter 2, in: *Physical Acoustics*, vol. 3B, ed. W.P. Mason (Academic Press, New York, 1965) 43-95.
- [5] D.H. Chung, Elastic moduli of single-crystal and polycrystalline MgO, *Phil. Mag.* 8, 89 (1963) 833-841.
- [6] O.L. Anderson and E. Schreiber, The pressure derivatives of the sound velocities of polycrystalline magnesite, *J. Geophys. Res.* 70 (1965) 5241-5248.
- [7] D.H. Chung, P.O. Benson, and W.B. Crandall, Elastic properties of polycrystalline magnesium-aluminate spinels, *Prog. Rept. No. 6*, Contract DA-31-124-ARO (D-23), Army Research Office, Durham, N.C. (1963).
- [8] E. Schreiber and O.L. Anderson, Pressure derivatives of the sound velocities of forsterite, with 6% porosity, *J. Geophys. Res.* 72 (1967a) 762-764; and a correction (1967b) 3751.
- [9] D.H. Chung and W. R. Buessem, The VHR approximation and the elastic moduli of polycrystalline ZnO, TiO₂, and α -Al₂O₃, *J. Appl. Phys.* 39 (1968) 2777-2782.
- [10] N. Soga and O.L. Anderson, Anomalous behavior of the shear sound velocity under pressure for polycrystalline ZnO, *J. Appl. Phys.* 38 (1967) 2985-2988.
- [11] N. Soga, Elastic properties of CaO under pressure and temperature, *J. Geophys. Res.* 73 (1968) 5385-5390.
- [12] R.C. Liebermann and E. Schreiber, Elastic constants of polycrystalline hematite, *J. Geophys. Res.* 73 (1968) 6585-6590.

- [13] D.H. Chung and G. Simmons, Pressure derivatives of the elastic parameters of quartz and rutile, *Earth Planet. Sci. Letters* 6 (1969) 134-138.
- [14] D.H. Chung, Effects of (Fe/Mg) ratio on P and S wave velocities in olivine, *J. Geophys. Res.*, *in press*, 75 (1970) 7353.
- [15] H. Fujisawa, Elastic Properties of polycrystalline olivine, *Trans. AGU* 51 (1970) 418 (abstract only).
- [16] H. Mizutani, Y. Hamano, Y. Ida, and S. Akimoto, Compressional-wave velocities in fayalite, Fe_2SiO_4 spinel, and coesite, *J. Geophys. Res.* 75 (1970) 2741-2747.
- [17] D.H. Chung and G. Simmons, The pressure and temperature derivatives of the elastic moduli of polycrystalline alumina, *J. Appl. Phys.* 39 (1968) 5316-5326.
- [18] J.K. Mackenzie, The elastic constants of a solid containing spherical holes, *Proc. Phys. Soc. (London)* 63B (1950) 2-11.
- [19] O.L. Anderson, E. Schreiber, R.C. Liebermann, and N. Soga, Some elastic constant data on minerals relevant to geophysics, *Rec. Geophys.* 6 (1968) 491-524.
- [20] J.B. Walsh, First pressure derivative of bulk modulus for porous materials, submitted to *J. Appl. Phys.*
- [21] W.F. Brace, Some new measurements of linear compressibility of rocks, *J. Geophys. Res.* 70 (1965) 391-398.
- [22] J.B. Walsh, The effect of cracks on the compressibility of rocks, *J. Geophys. Res.* 70 (1965) 381-390.
- [23] A. Nur and G. Simmons, The origin of small cracks in igneous rocks, *Int. J. Rock Mech. Min. Sci.* 7 (1970) 307-314.
- [24] N.A. Weil, Parametric effects governing the mechanics of ceramic materials, in: *High Temperature Technology*, ed. N.K. Hiester (Butterworth Publishers Inc., Washington, D.C., 1964), 189-233.
- [25] F. Birch, Compressibility; elastic constants, in: *Handbook of Physical Constants*, Geol. Soc. Am. Memoir 97, ed. S.P. Clark Jr., Section 7 (1966).
- [26] D.H. Chung, Elasticity and equations of state of olivine: Effects of the iron/magnesium ratio, to be published. *JGR*
- [27] E.K. Graham, Jr., and G.R. Barsch, Elastic constants of single-crystal forsterite as a function of temperature and pressure, *J. Geophys. Res.* 74 (1969) 5949-5960.
- [28] M. Kumazawa and O.L. Anderson, Elastic moduli, pressure derivatives, and temperature derivatives of single-crystal olivine and single-crystal forsterite, *J. Geophys. Res.* 74 (1969) 5961-5972.
- [29] E. Schreiber and O.L. Anderson, Pressure derivatives of sound velocities of polycrystalline alumina, *J. Am. Ceram. Soc.* 49 (1966) 184-190.
- [30] J.H. Gieske and G.R. Barsch, Pressure dependence of the elastic constants of single-crystalline aluminum oxide, *Phys. Status Solidi* 29 (1968) 121-131.
- [31] M.H. Manghani, Elastic constants of single-crystal rutile under pressure to 7.5 kb, *J. Geophys. Res.* 74 (1969) 4317-4328; correction in *J. Geophys. Res.* 75 (1970) 2151.
- [32] O.L. Anderson and R.C. Liebermann, Elastic constants of oxide compounds used to estimate the properties of the earth's interior, in: *On the Application of Modern Physics to the Earth and Planetary Interiors*, ed. S.K. Runcorn (Wiley, New York, 1969), pp. 425-448.
- [33] D.H. Chung and G. Simmons, Elastic properties of polycrystalline periclase, *J. Geophys. Res.* 74 (1969) 2133-2135.
- [34] E. Schreiber and O.L. Anderson, Revised data on polycrystalline MgO, *J. Geophys. Res.* 73 (1968) 2837-2838.
- [35] N. Soga, Elastic constants of BeO as a function of pressure and temperature, *J. Am. Ceram. Soc.* 52 (1969) 246-249.
- [36] J.B. Wachtman, Jr., W.E. Tefft, D.G. Lam, Jr., and R.P. Stinchfield, Elastic constants of synthetic single-crystal corundum at room temperature, *J. Res. NBS (USA)* 64 A (1960) 213-228.